

Collaborating with



UNIVERSITÉ
DE GENÈVE



A ROBUST ENERGY SYSTEM UNDER UNCERTAINTY: MULTI-LEVEL OPTIMIZATION-BASED FRAMEWORKS

Presented by
Amin Abedi

*Institute for Environmental Sciences (ISE), UNIGE, Switzerland
Laboratory of signal and risk analysis
Energy department, Politecnico di Milano, Italy*

A brief bio



Intro

AC based
approach

Vulnerability
& uncertainty

Questions

- **Ongoing–Postdoc researcher (Remotely in Ann Arbor)**

Politecnico di Milano, Energy department, Laboratory of signal and risk analysis

Prof. Enrico Zio (lab leader)

Topic of research: Enhancing the Robustness of the IEGS Considering the Bidirectional Physical-Economic Interdependencies: A Quasi Steady-State Multilevel Optimization Model.

- **PhD in Science- Environmental Science-Energy section (Defended, 31.03.2021)**

Institute for Environmental Sciences, University of Geneva, Switzerland

Topic of research: Optimization-based Frameworks for Systemic Vulnerability Assessment in the Electric Power Systems.

- **M.Sc. in Energy Engineering,**

Sharif university of technology, ENERGY Department

- **B.Sc. in Electrical Engineering-power electrical engineering**

Power system and its different hazards

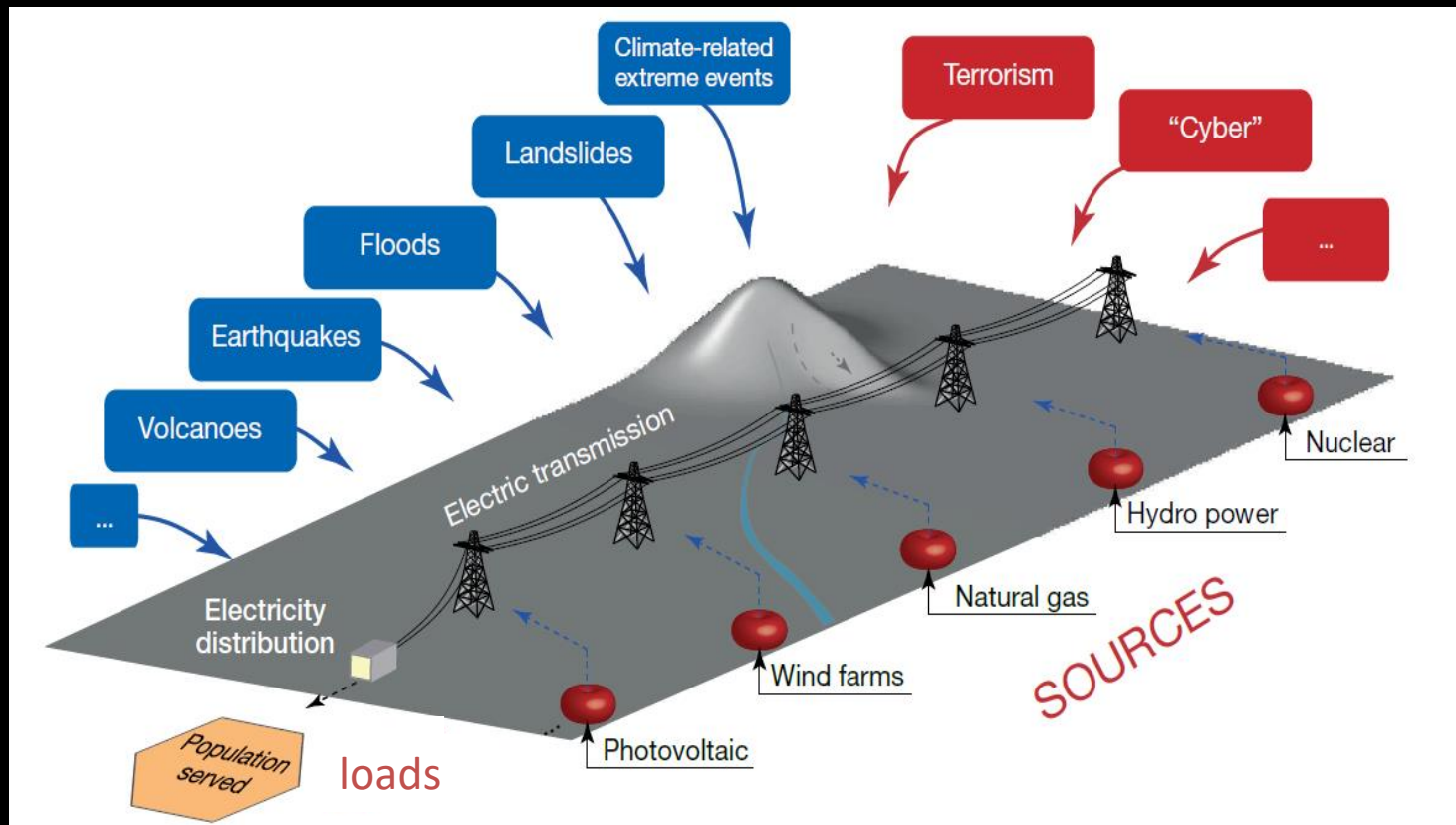


Intro

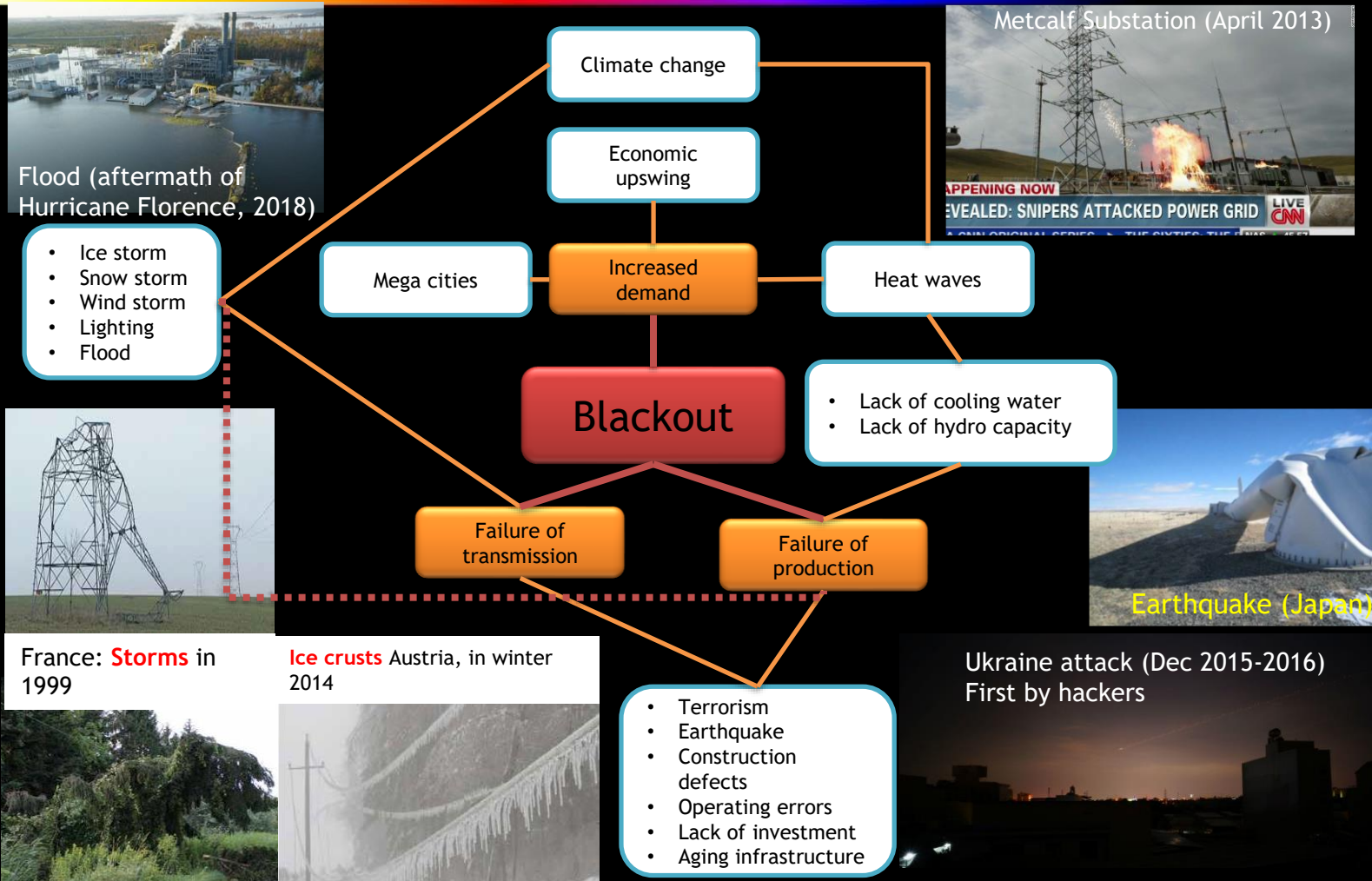
AC based
approach

Vulnerability
& uncertainty

Questions



Power system and High-impact, Low-probability Events



Blackout: the loss of supply to the load in the entire power system, or parts of the system,
Cascading failures: a sequence of dependent outages of individual components that successively weakens the power system.

Economic loss to sense the consequences

No.	Country	Year	Load loss (GW)	Economic loss	People affected (*Million)
1	USA, Canada	2003	61.8	\$ 6.4 billion	50
2	Italy	2003	24	Over €120 million	~56
3	Russia	2005	~3.5	\$ 1-2 billion	4
4	USA and Mexico	2011	4.3	Up to \$118 million	Over 5

In the USA, the annual cost of weather-related blackouts ranges from **\$20 to \$55 billion**.



VSE reported the costs of a blackout which is **2-4 billion** CHF per day. For comparison, the Swiss GDP per day was (2012) **2.4** billion CHF.



Intro

AC based approach

Vulnerability & uncertainty

Questions

So...



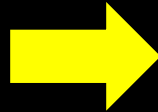
Intro

AC based approach

Vulnerability & uncertainty

Questions

The past blackout reports



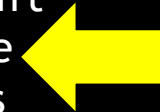
N-1 criteria is not enough

~~COST EFFECTIVE~~

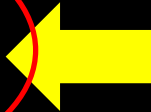
Secure for all possible outages



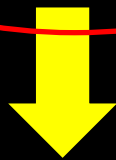
lessons learned from the past blackouts



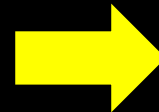
The outages don't have the same consequences



Find combinations of assets that their simultaneous outages cause more damage to the system (N-2, N-3,...)



Focus on those **Critical assets** that their simultaneous outages lead to major damage and then try to harden them “proactively” based on their exposed hazards

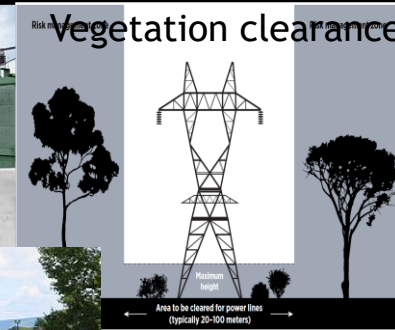


Floodgates

Measures to harden infrastructure



Flood walls



Adding assets VS. Braess paradox

N-1 security criterion: If any single component fails, the loads can be restored without load shedding

Ref: https://en.wikipedia.org/wiki/North_American_power_transmission_grid

Arulampalam Atputharajah, Tapan Kumar Saha, Power System Blackouts - Literature review, 2009

So...



Intro

AC based
approach

Vulnerability
& uncertainty

Questions

Find combinations of assets
that their simultaneous
outages cause more damage
to the system (N-2,N-3,...)



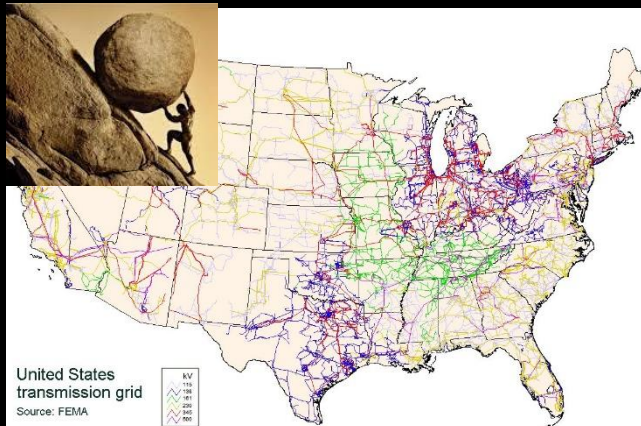
Introducing an index and
ranking all assets based on
that index OR enumeration

Developing models to
directly find the worse case
scenario or the critical
assets

N=1000

N-1=1000 cases
N-2=499000 cases
N-3=160 million cases
N-4=40 billion cases
...

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$



Follower

Leader

Methods for Vulnerability analysis



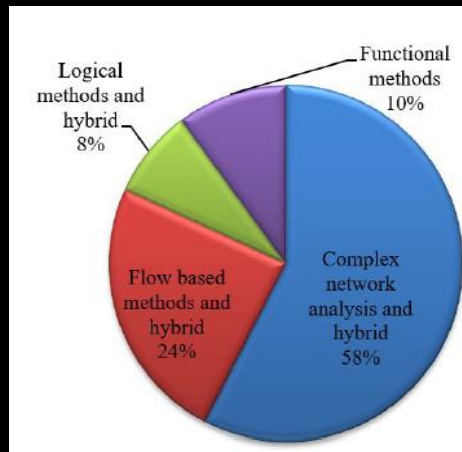
Intro

AC based approach

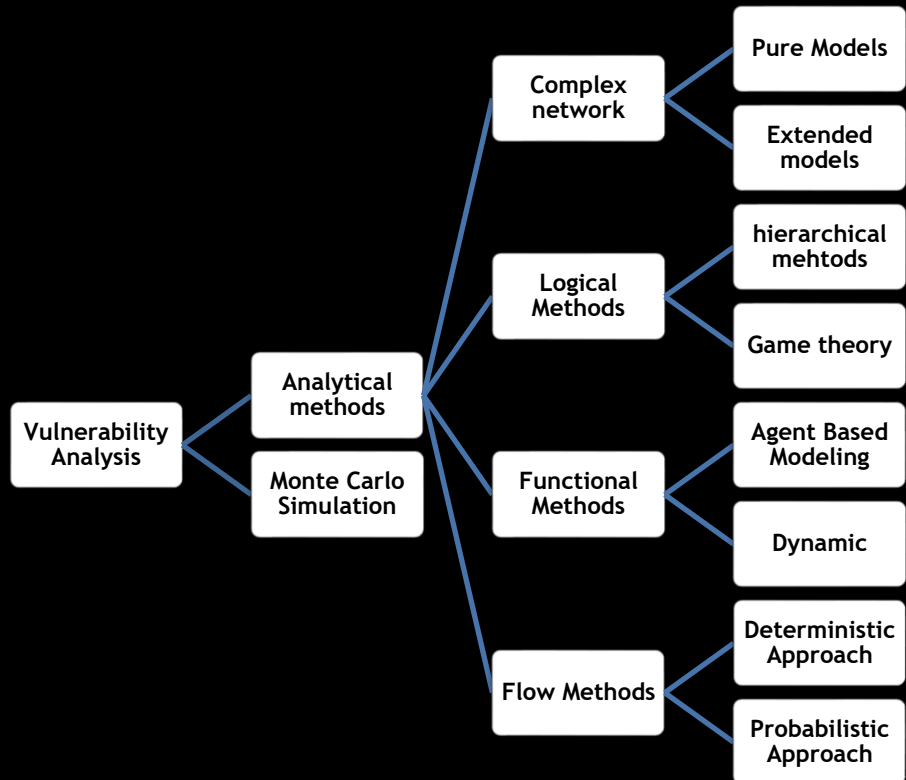
Vulnerability & uncertainty

Questions

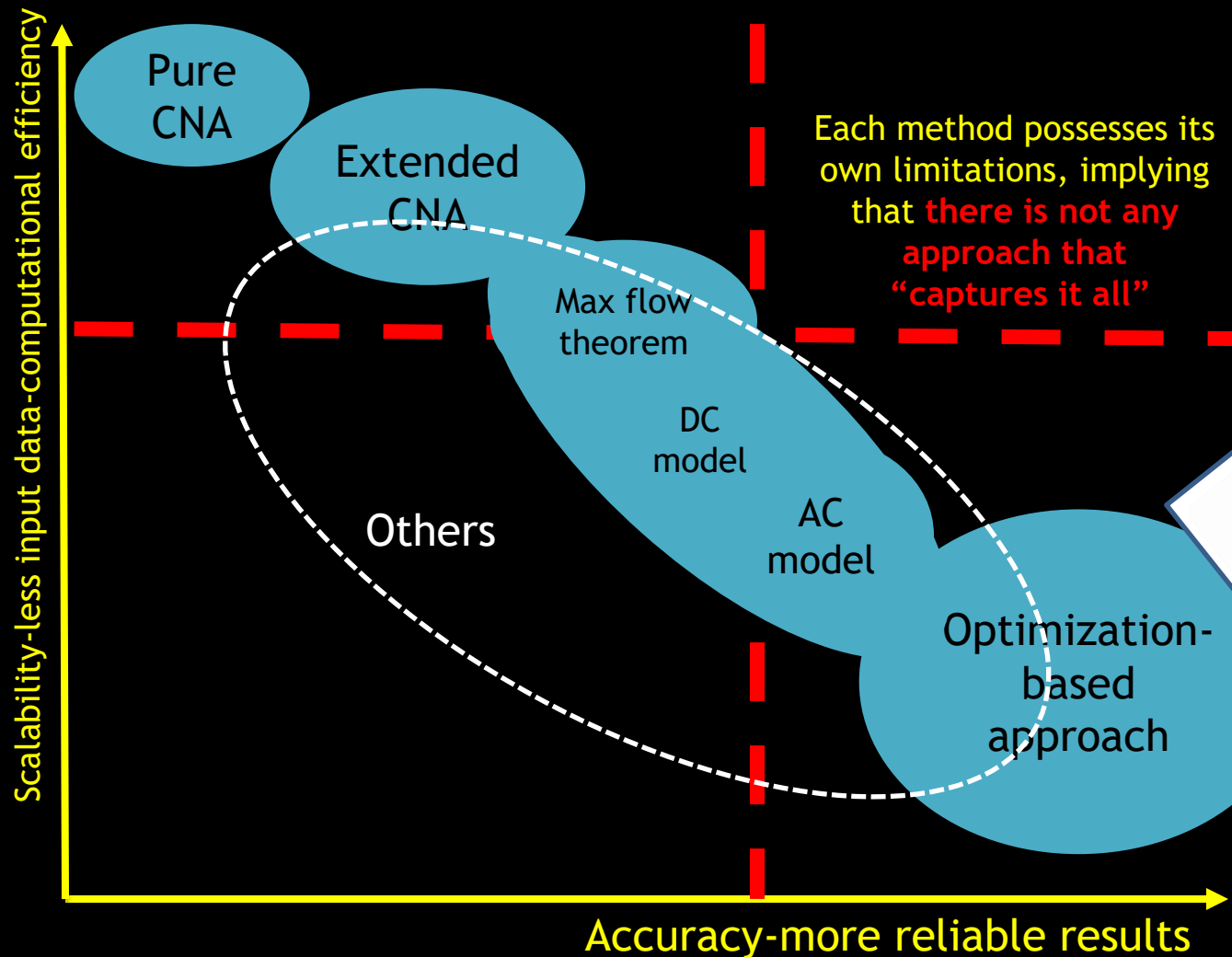
About 300 articles reviewed and about 100 summarized in four tables



- ❖ The methodology used,
- ❖ Assumptions,
- ❖ Test cases,
- ❖ Failure scenarios, and
- ❖ Modeling capability



Comparison of methods



Leader-follower approach as a good solution

Follower

(3) Follower observes
the leader's action
and adapts its strategy
so as to minimize its
own cost

(2) Leader
announces its
strategy

(4) Follower
announces its
strategy

Leader

(1) Leader
optimizes its
strategy given the
follower's actions

Follower



Leader

Leader-follower approach as a good solution



Intro

AC based
approach

Vulnerability
& uncertainty

Questions

Follower

Leader

Consumer

Economy

Producer

Factory owner

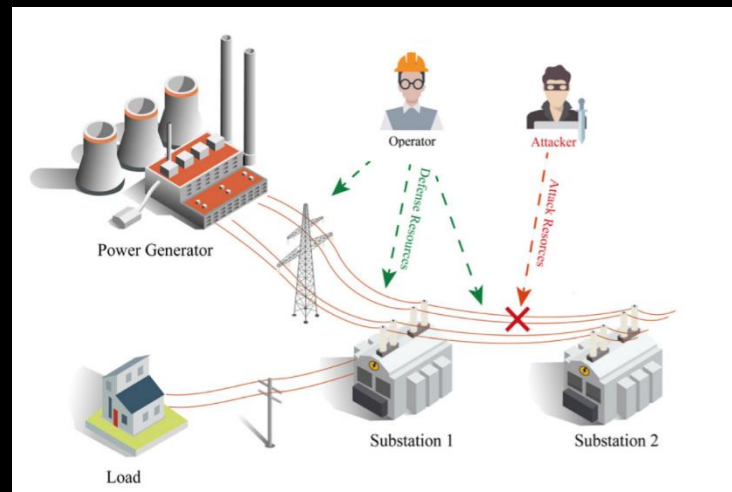
Taxation

Government

Defender

Security

Attacker



Leader-follower approach as a good solution



General form of a bilevel problem to show a leader follower structure

$$\min_{x \in X} F(x, y) = c_1 x + d_1 y$$

$$\text{subject to } A_1 x + B_1 y \leq b_1$$

$$\min_{y \in Y} f(x, y) = c_2 x + d_2 y$$

$$\text{subject to } A_2 x + B_2 y \leq b_2$$

An optimization problem that contains another optimization problem as a constraint

A real bilevel example

$$\begin{aligned} \min_{x \in X} F(x, y) &= c_1 x + d_1 y \\ \text{subject to } A_1 x + B_1 y &\leq b_1 \\ \min_{y \in Y} f(x, y) &= c_2 x + d_2 y \\ \text{subject to } A_2 x + B_2 y &\leq b_2 \end{aligned}$$

These problems are also known as the hierarchical leader-follower problem or Stackelberg game.

AC-OPF



$$\text{Max}_z \sum_{i \in N} Ls_i^*$$

→ Total load shedding

$$\text{s.t. } 0.5 \times \sum_{i,j \in N} (1 - z_{ij}) = NPO; \quad z_{ij} \in \{0, 1\} \quad \forall i, j \in N$$

$$z_{ij} = z_{ji}; \quad z_{ij} \in \{0, 1\} \quad \forall i, j \in N$$

MIBNLP

$$\text{where: } \sum_{i \in N} Ls_i^* \in \arg \left\{ \text{Min}_{\substack{P_g, Q_g, Ls, Lsq, \\ P, Q, V, \theta}} \sum_{i \in N} Ls_i \right\}$$

$$\text{s.t. } Pg_{ij \in G} + Lsq_{ij \in D} - Pd_{ij \in D} = \sum_{j \in N} P_j; \quad \forall i, j \in N: (\alpha_i)$$

$$Qg_{ij \in G} + Lsq_{ij \in D} - Qd_{ij \in D} = \sum_{j \in N} Q_j; \quad \forall i, j \in N: (\beta_i)$$

$$P_j = z_{ij} \left(V_i^2 G_{ij} - V_i V_j (G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij}) \right); \quad \forall i, j \in N: (\lambda_{ij})$$

$$Q_j = z_{ij} \left(-V_i^2 \left(B_{ij} + \frac{B_{ij}^{sh}}{2} \right) - V_i V_j (G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij}) \right);$$

$$\forall i, j \in N: (\mu_{ij})$$

$$0 \leq Pg_i \leq Pg_i^{\max}; \quad \forall i \in G: (\bar{\sigma}_i)$$

$$Qg_i^{\min} \leq Qg_i \leq Qg_i^{\max}; \quad \forall i \in G: (\underline{\sigma}_i, \bar{\sigma}_i)$$

$$(P_j)^2 + (Q_j)^2 \leq (S_j^{\max})^2; \quad \forall i, j \in N$$

$$V_i^{\min} \leq V_i \leq V_i^{\max}; \quad \forall i \in N: (\underline{v}_i, \bar{v}_i)$$

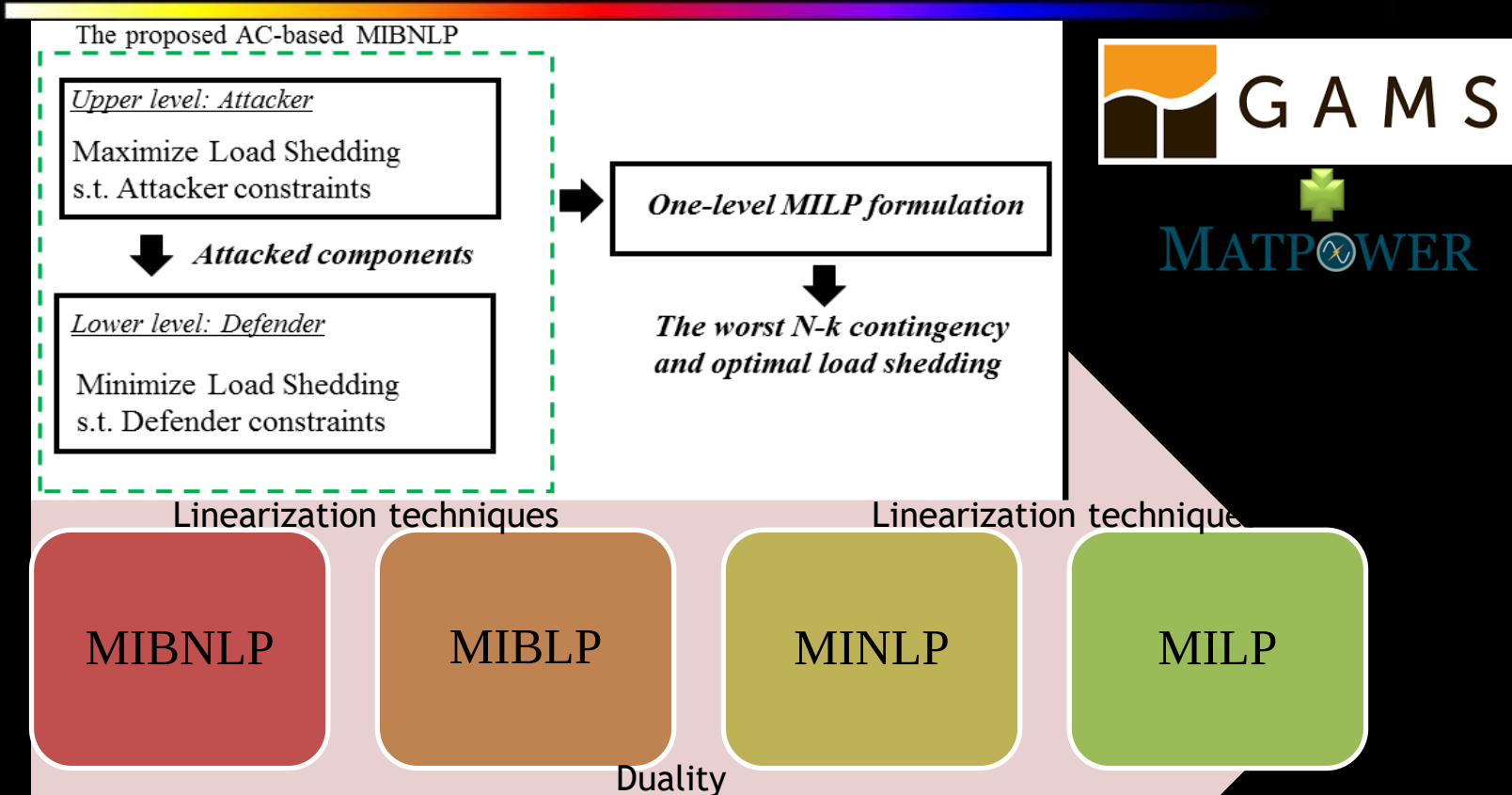
$$\theta_j^{\min} \leq \theta_j \leq \theta_j^{\max}; \quad \forall i, j \in N$$

$$0 \leq Ls_i \leq Pd_i; \quad \forall i \in D: (\bar{\omega}_i)$$

$$Lsq_i = Ls_i \tan \phi_i; \quad \forall i \in D$$

Non linear equations

Methods and scenarios



MIBNLP = mixed-integer bilevel nonlinear program,
MIBLP = mixed-integer bilevel linear program,
MINLP = (single-level) mixed-integer nonlinear program,
MILP = mixed-integer linear program,
GAMS= General Algebraic Modeling System platform

Linearization techniques

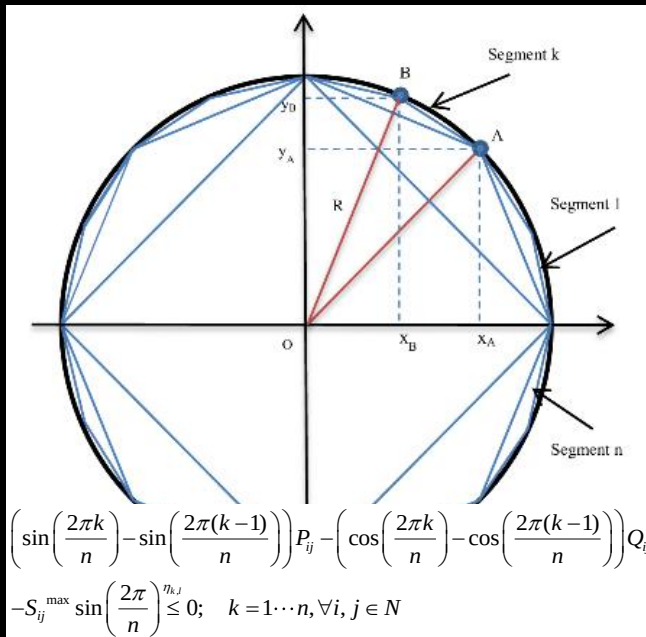
$$(P_{ij})^2 + (Q_{ij})^2 \leq (S_{ij}^{\max})^2; \quad \forall i, j \in N$$

$$P_{ij} = z_{ij} (V_i^2 G_{ij} - V_i V_j (G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij})); \quad \forall i, j \in N: (\lambda_{ij})$$

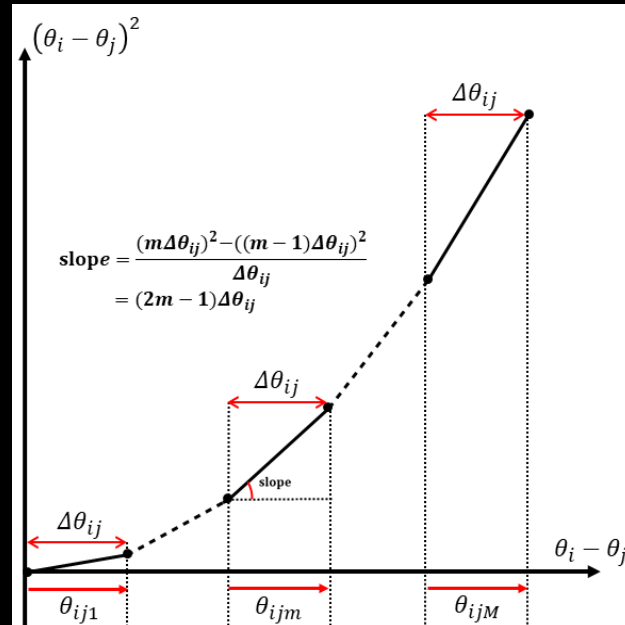
$$Q_{ij} = z_{ij} \left(-V_i^2 (B_{ij} + \frac{B_{ij}^{sh}}{2}) - V_i V_j (G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij}) \right);$$

Bilinear terms

N-sided convex regular polygon



Piecewise linear (PWL)



Big-M technique

Test systems



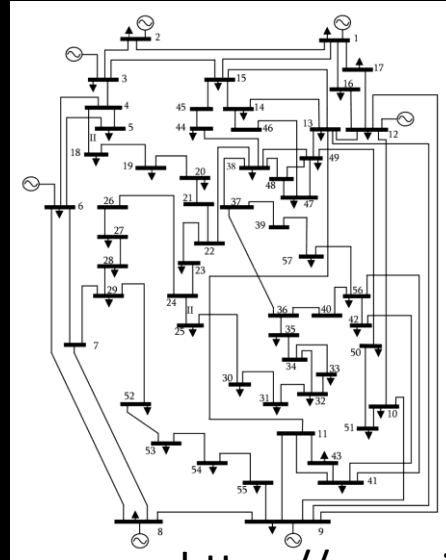
Intro

AC based
approach

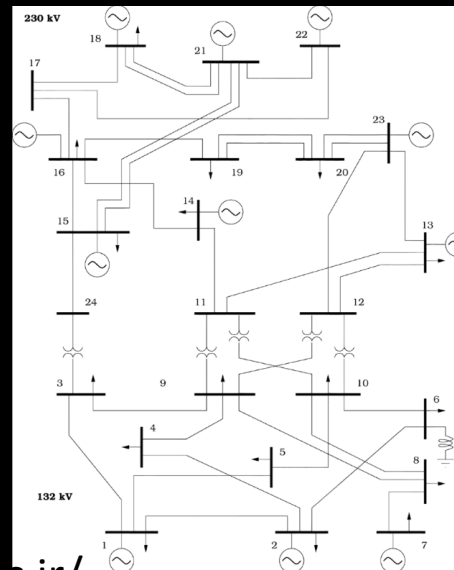
Vulnerability
& uncertainty

Questions

IEEE 57-bus :
57 buses, 7
generators,
and 80
branches and
transformers



IEEE 24-bus
reliability test
systems (RTS):
24 buses, 32
generators, and 38
branches and
transformers



IEEE 57-bus system

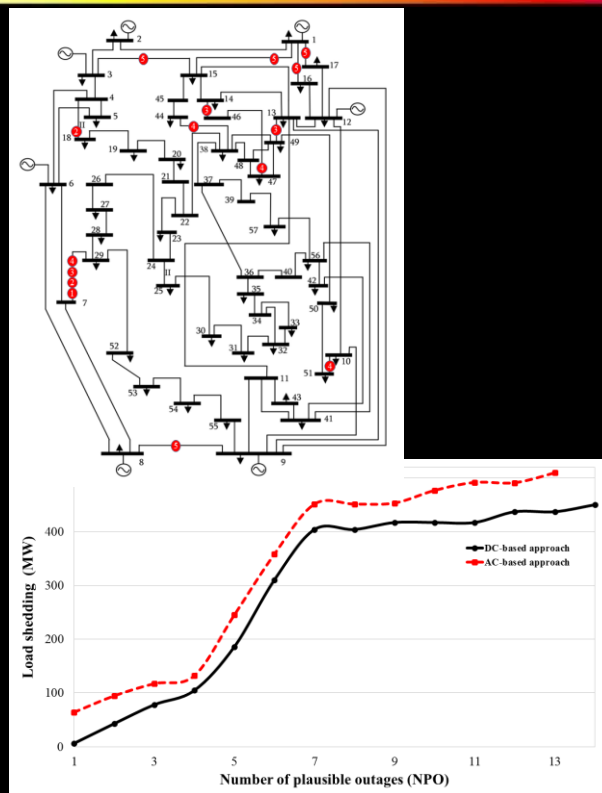


Intro

AC based approach

Vulnerability & uncertainty

Questions



NPO	DCOPF-based approach*	LS (MW)	ACOPF-based approach	LS (MW)	JSI
1	25-30	6	7-29	64	0
2	1-16, 12-16	43	4-18, 7-29	95	0
3	7-29, 9-55, 21-22	78	7-29, 13-49, 14-46	118	0.2
4	7-29, 8-9, 12-17, 21-22	105	7-29, 10-51, 38-44, 46-47	132	0.1
5	1-16, 7-29, 8-9, 12-17, 21-22	186	1-15, 1-16, 1-17, 3-15, 8-9	245	0.3

* This approach is also used with different objective functions and case studies in [347, 352-354].

The five worst-case load shedding scenarios and their related lines for the IEEE 57-bus system calculated using our MILP model

Trigger point for Chapter 6 (Peak load and Load profile)



Peak load



Load
profile

Methods and scenarios

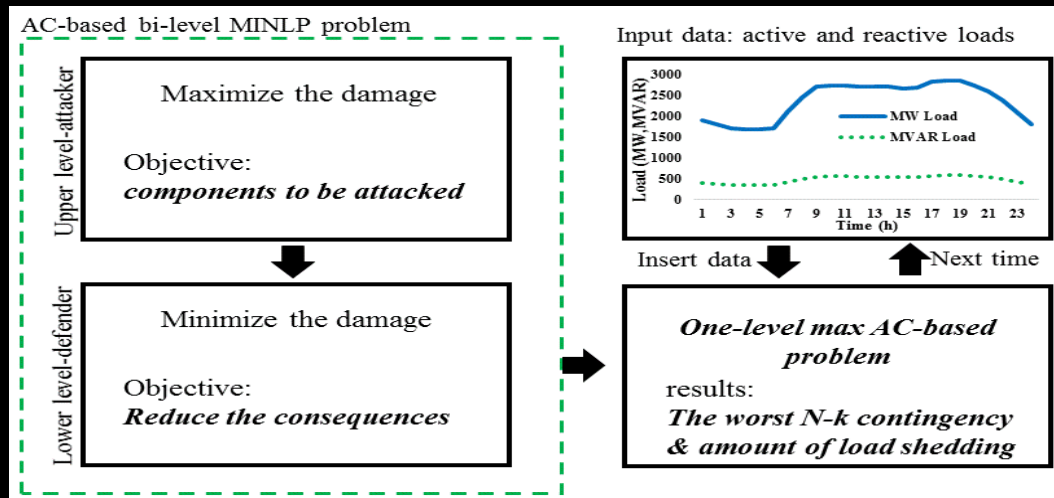


Intro

AC based approach

Vulnerability & uncertainty

Questions



Linearization techniques

MIBNLP

MIBLP

MINLP

MILP

Duality theory

MIBNLP=mixed-integer bilevel nonlinear program,
 MIBLP = mixed-integer bilevel linear program,
 MINLP = (single-level) mixed-integer nonlinear program,
 MILP = mixed-integer linear program,
 GAMS= General Algebraic Modeling System platform

Test system

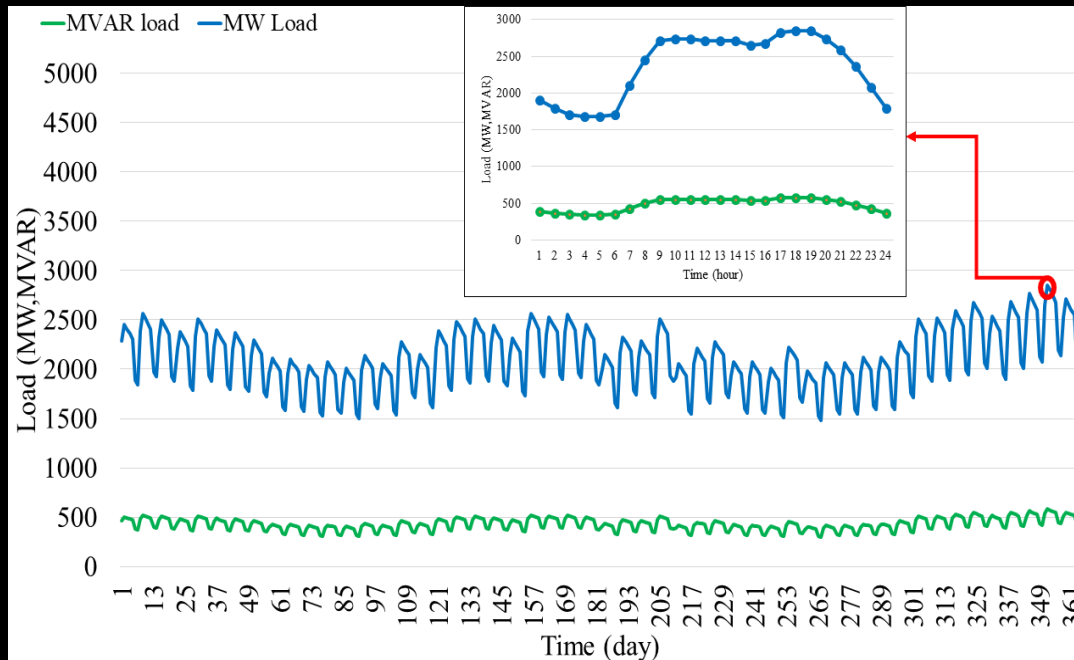


Intro

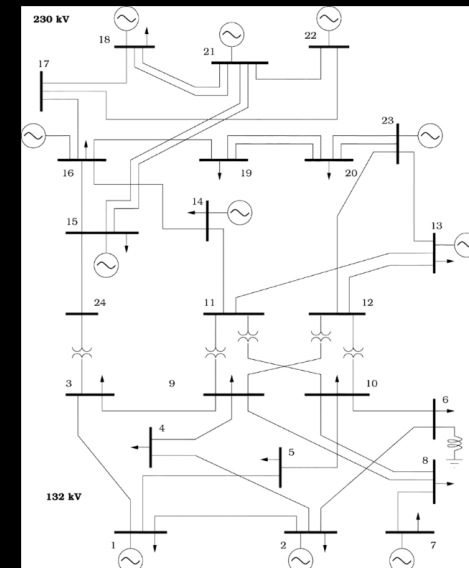
AC based
approach

Vulnerability
& uncertainty

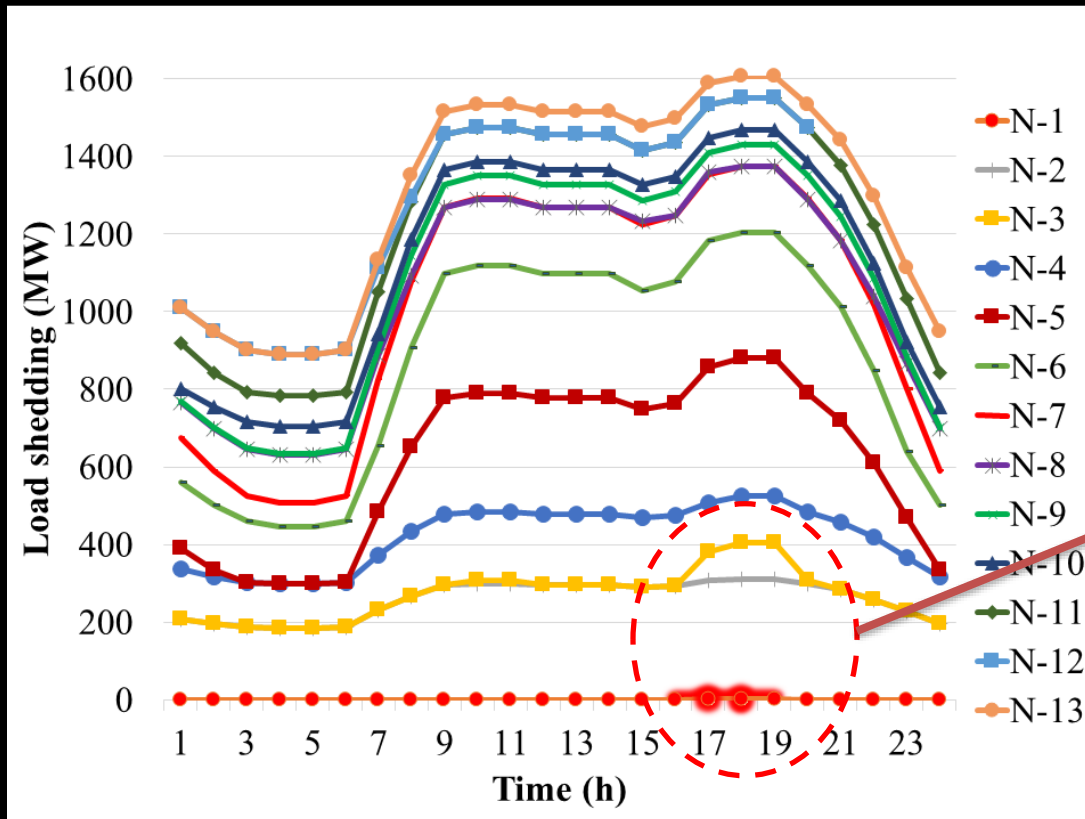
Questions



IEEE 24-bus
reliability test
systems (RTS):
24 buses, 32
generators, and 38
branches and
transformers



Effects of the contingencies with hourly peak loads



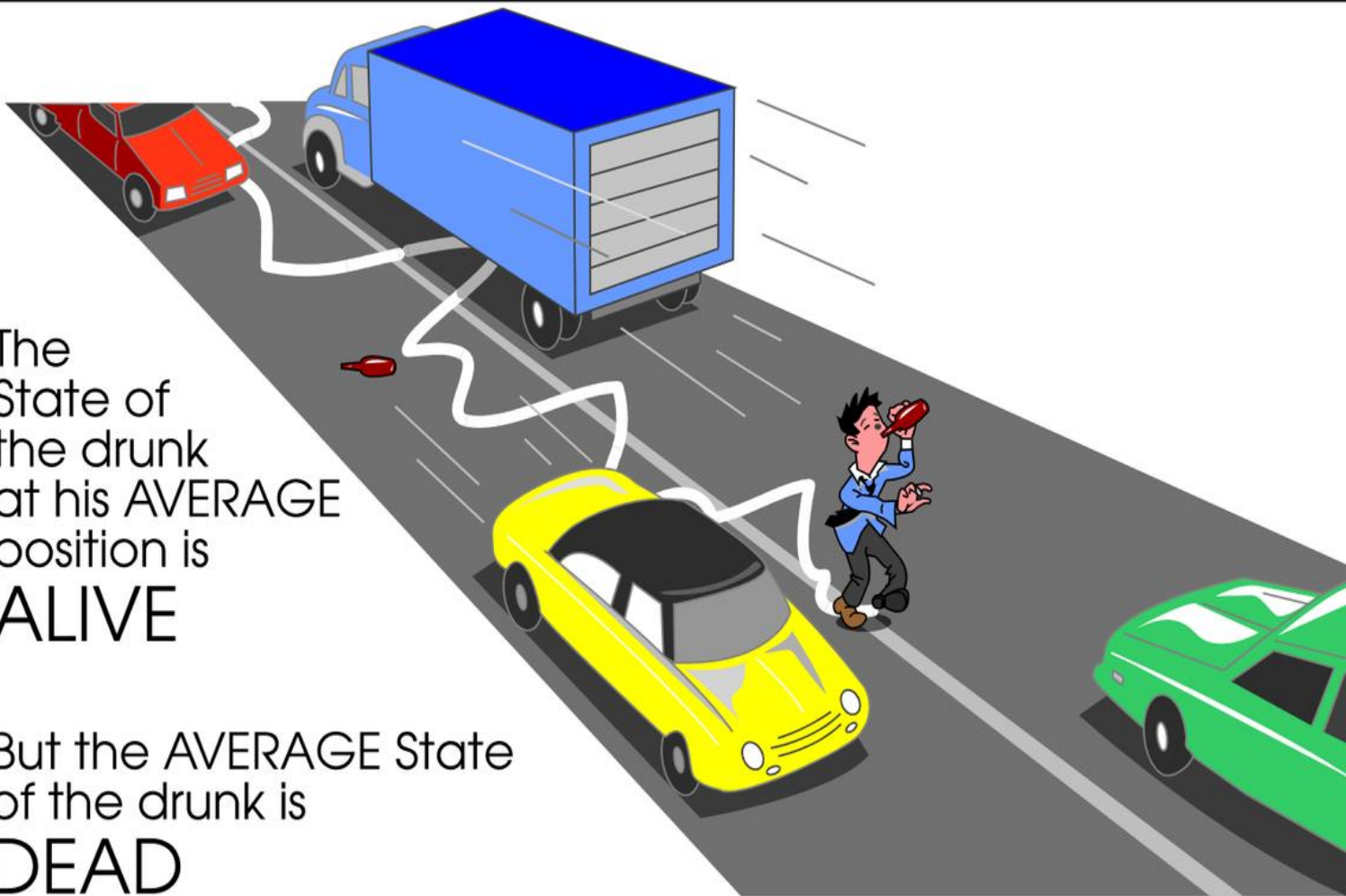
Let us to use load management or even increasing efficiency as one of the measures for increasing robustness.

“where and which” as well as “when” the system is more vulnerable?

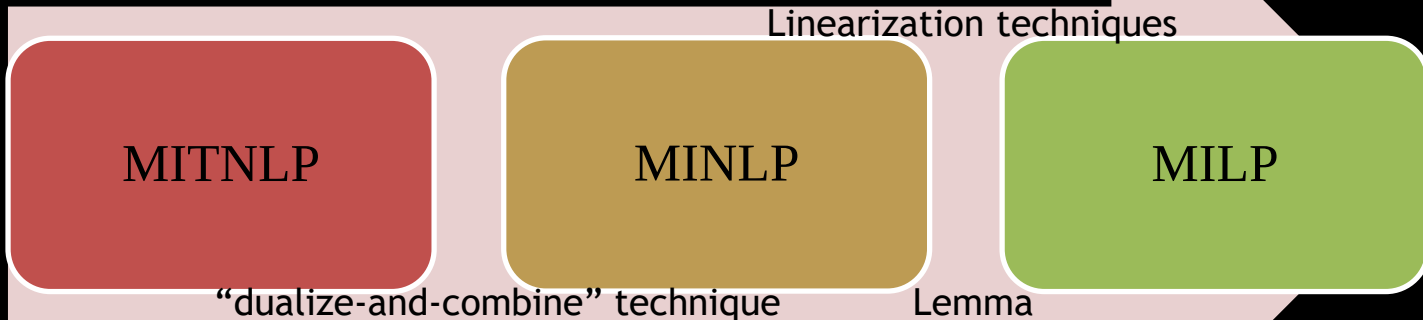
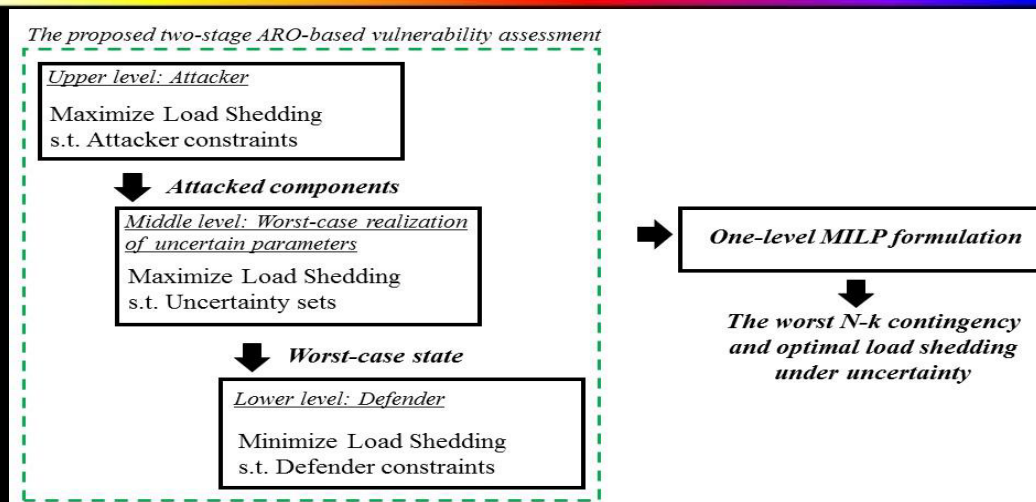
Trigger point
(Security assessment and average data)

The
State of
the drunk
at his AVERAGE
position is
ALIVE

But the AVERAGE State
of the drunk is
DEAD



Methods and scenarios



MITNLP =mixed-integer trilevel nonlinear program,
MINLP =(single-level) mixed-integer nonlinear program,
MILP =mixed-integer linear program,
GAMS= general algebraic modeling system platform



Intro

AC based approach

Vulnerability & uncertainty

Questions

Formulation and Uncertainty Characterization



Intro

AC based
approach

Vulnerability
& uncertainty

Questions

$$\underset{z}{\text{Maximize}} \sum_{i \in N} Ls_i^{**} \quad (7-2)$$

$$\text{subject to: } 0.5 \times \sum_{i,j \in N} (1 - z_{ij}) = NPO; \quad z_{ij} \in \{0,1\} \quad \forall i,j \in N \quad (7-3)$$

$$z_{ij} = z_{ji}; \quad z_{ij} \in \{0,1\} \quad \forall i,j \in N \quad (7-4)$$

$$\text{where: } \sum_{i \in N} Ls_i^{**} \in \arg \left\{ \underset{\bar{P}_g, \bar{P}_d}{\text{Maximize}} \sum_{i \in N} Ls_i^* \right\} \quad (7-5)$$

$$\text{subject to: } \bar{P}g_i - \hat{P}g_i \leq \tilde{P}g_i \leq \bar{P}g_i + \hat{P}g_i; \quad \forall i \in G \quad (7-6)$$

$$\sum_{i \in G} \left| \frac{\tilde{P}g_i - \bar{P}g_i}{\hat{P}g_i} \right| \leq DR^g; \quad \forall i \in G \quad (7-7)$$

$$\bar{P}d_i - \hat{P}d_i \leq \tilde{P}d_i \leq \bar{P}d_i + \hat{P}d_i; \quad \forall i \in D \quad (7-8)$$

$$\sum_{i \in D} \left| \frac{\tilde{P}d_i - \bar{P}d_i}{\hat{P}d_i} \right| \leq DR^d; \quad \forall i \in D \quad (7-9)$$

Uncertainty
definition:

$$\text{where: } \sum_{i \in N} Ls_i^* \in \arg \left\{ \underset{\substack{\bar{P}_g, Ls_i^*, \\ \bar{P}_d, \theta}}{\text{Minimize}} \sum_{i \in N} Ls_i \right\} \quad (7-10)$$

$$\text{subject to: } P_{g_{ij \in G}} + Ls_{ij \in D} - \tilde{P}d_{ij \in D} = \sum_{j \in N} P_{ij}; \quad \forall i \in N: (\lambda_i) \quad (7-11)$$

$$P_{ij} = z_{ij} B_{ij} \theta_{ij}; \quad \theta_{ij} = \theta_i - \theta_j; \quad \forall i,j \in N: (\mu_{ij}) \quad (7-12)$$

$$0 \leq P_{g_i} \leq \tilde{P}g_i; \quad \forall i \in G: (\gamma_i) \quad (7-13)$$

$$-S_{ij}^{\max} \leq P_{ij} \leq S_{ij}^{\max}; \quad \forall i,j \in N: (\varphi_{ij}, \bar{\varphi}_{ij}) \quad (7-14)$$

$$-\theta_i^{\max} \leq \theta_i \leq \theta_i^{\max}; \quad \forall i \in N: (\omega_i, \bar{\omega}_i) \quad (7-15)$$

$$0 \leq Ls_i \leq \tilde{P}d_i; \quad \forall i \in D: (\bar{\alpha}_i) \quad (7-16)$$

- Two set of equations for loads and generations,
- DRs are the budget of uncertainty,
- an interval

The lemma and its results

$$\underset{\substack{\lambda_i, \mu_{ij}, \alpha_i, \omega_i, \\ \underline{\omega}_i, \gamma_i, \underline{\varphi}_{ij}, \varphi_{ij}}}{\text{Maximize}} \left(\sum_{i \in N} (\lambda_i + \bar{\alpha}_i) \tilde{P} d_{i|i \in D} + \sum_{i \in G} \bar{\gamma}_i \tilde{P} g_i + \sum_{i, j \in N} (\bar{\varphi}_{ij} - \underline{\varphi}_{ij}) S_{ij}^{\max} + \sum_{i \in N} (\bar{\omega}_i - \underline{\omega}_i) \theta_i^{\max} \right)$$

Products of two continuous variables

lemma: “An optimal solution of the middle problem is when the uncertain parameters reach either upper or lower bounds.”

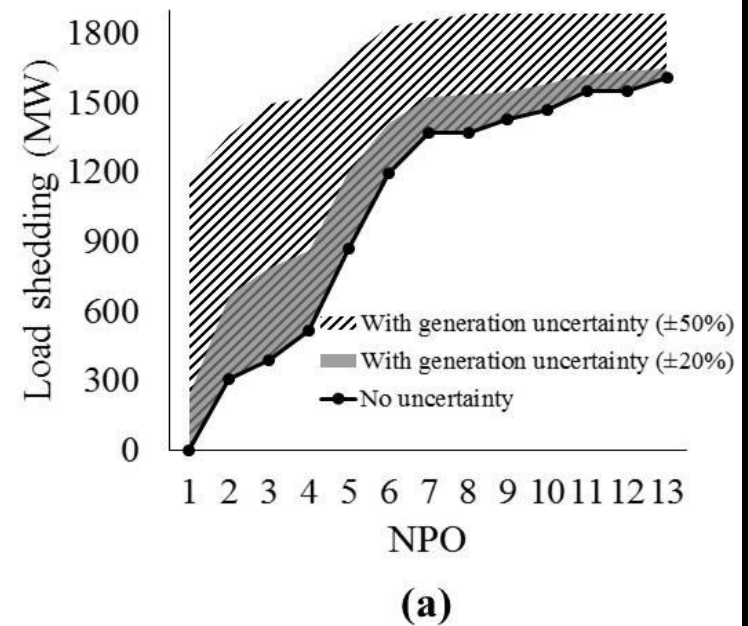
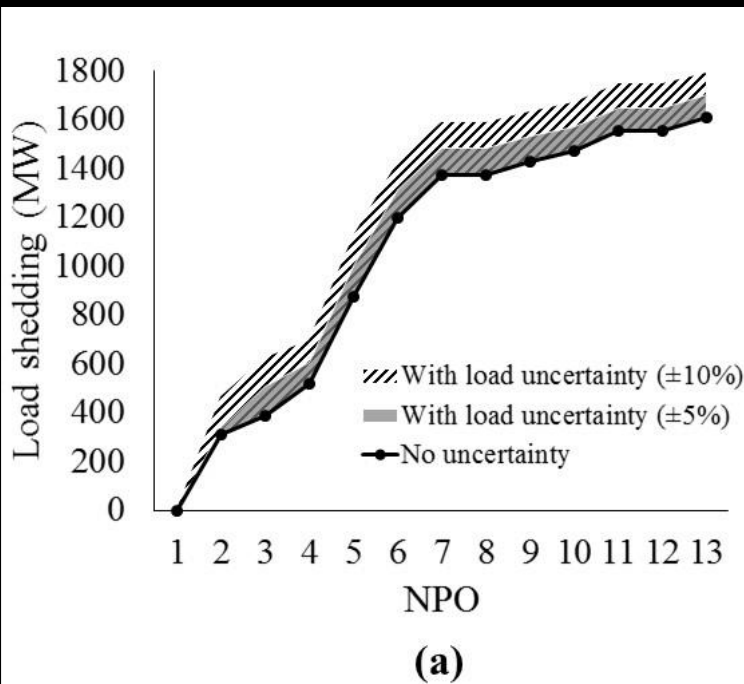
Model statistics		Binary expansion formulation	Extreme points
Single equations		3121	↔ 1046
Single variables		1906	↔ 766
Binary variables		409	↔ 130
	scenario I	5.2	↔ 0.9
	scenario II	11.2	↔ 0.8
	scenario III	7.4	↔ 2.1
Average elapsed time/simulation (sec)*	scenario IV	2.8	↔ 0.7
	scenario V	553	↔ 3.0
	scenario VI	471	↔ 2.1

*In all scenarios, NPO is fixed to 13.

Vulnerability analysis with load and generation separately

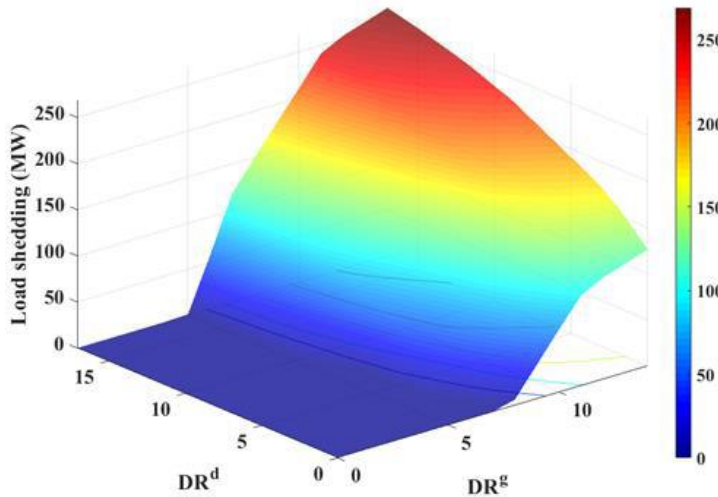
- ❑ Load variation: 5%-10%,
- ❑ The uncertainty budget: 0-17,
- ❑ The maximum differences: 30% and 60% when NPO=3,
- ❑ The results without uncertainty is optimistic, and proposing different critical lines.

- ❑ Generation variation : 20 % and 50 %,
- ❑ The uncertainty budget: 0-14,
- ❑ The maximum differences: 118% and 342%, when NPO=1,
- ❑ The results without uncertainty is optimistic, and proposing different critical lines .

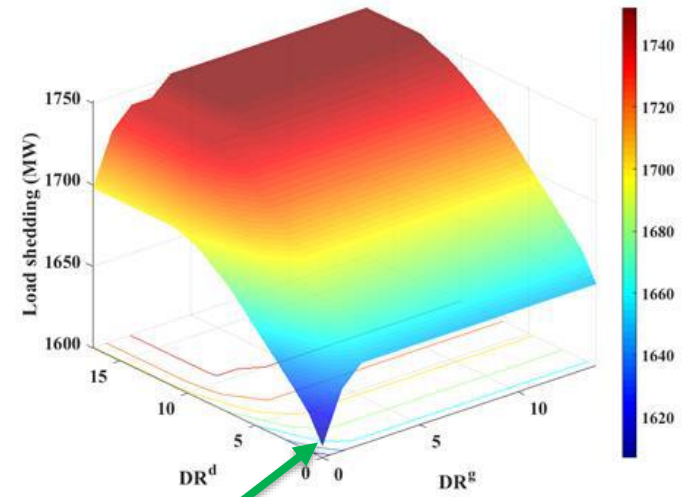


Vulnerability analysis with both uncertainties

The results without uncertainty is optimistic, and proposing different critical lines .



NPO=0



NPO=13

What we
have from
the model
???

DR^g = DR^d =NPO	Critical lines	Generation unit*	Load bus number*	LS (MW)
1	-	-	-	0
2	15-21,16-17	G6,G14	13,15	429
3	7-8,15-21,16-17	G6,G13,G14	10,13,15	676
4	3-24,12-23,13-23,14-16	G2,G4,G5,G6	3,10,13,14	797
5	12-23,13-23,15-21,16-17,20-23	G4,G5,G6,G8,G9	10,13,14,15,19	1200
6	11-13,12-13,12-23,15-21,16-17,20-23	G2,G4,G5,G7,G8,G9	3,9,10,14,15,19	1455

* In these components, when the uncertain parameters reach the boundary of their intervals, the worst-case scenario occurs.

Thank you for your time and attention



Intro

AC based
approach

Vulnerability
& uncertainty

Questions

